

Technique of tooth relieving of worm hobs for cutting Novikov gears with double lines of action

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Abstract. Worm hobs for cutting Novikov gears have the profile of a generating worm, which varies not only in a radius, but also in a sign of curvature. A technique for relieving tooth flanks of these hobs by disk grinding wheel is developed. It allows for bringing together grinding and ground profiles in an axial section of the generating worm as close as possible. A method for calculating setting-ups and profile coordinates of the grinding wheel is given for real production conditions.

KEY WORDS: WORM HOBS, GRINDING, RELIEVING, TOOTH PROFILE, NOVIKOV GEARS.

Introduction

Formation of screw and relieved surfaces by disk grinding wheels includes inevitable deviation of ground surface and wheel profiles. Such a deviation was called an organic error. For a straight basic rack the organic error has to be minimized as much as possible or the obtained profile is taken as the basic rack at the attained degree of minimization [1-3]. For the screw and relieved surfaces when a profile has a substantial and variable curvature, this organic error must be eliminated to the maximum degree.

This problem was solved in a well-known example for the unruled worm of ZT2 type, proposed by F.L. Litvin in 1961 (later, in the monograph [4] such worms are considered as worms ZF-II type). An axial profile of the grinding wheel was set in the form of a circle arc, and then an angle of installation of the grinding wheel axis and an axial profile of a worm thread were sought based on the condition that this arc was a contact line of the wheel and the ground surface. Obviously, a solution of an inverse problem is required to obtain a worm hob with relieved surfaces of teeth being close to the found worm thread profile.

In [2, 5], authors proposed the solution of a similar problem for gears with liquid friction with respect to the convex thread profile of a worm and a hob for cutting teeth. It was specified for the substantially curvilinear axial profile of the working worm (or the hob generating worm) and also taking into account a profile of a grinding wheel in the axial section of the worm. The setting angle of the grinding wheel axis was determined from the condition that this axis intersects two normal lines to the thread axial profile and it is located in a plane parallel to the axis of the worm. The proposed method ensures minimization of the organic error in the profiling of the worm thread. Similar organic error in tool profiling was accounted, because of the necessary identity of the profile of the hob generating worm.

In [6] authors made the first attempt to apply general principles of this method to the study of the relieving process of worm hobs for cutting Wildhaber-Novikov gears. In this case, two significant factors were taken into account. At first, a profile curvature of a generating rack of these worm hobs is a variable not only in a radius of curvature, but also in its sign. At second, the possibilities of a relieving machine allow for setting the axis of a grinding wheel in a plane not parallel to the axis of the ground product; it improves grinding conditions for a number of parameters.

In the present work, this research is developed and continued. It solved the main issues of relieving technique that are functionally oriented for solving the following problems: providing rear angles of the teeth necessary for the wear resistance of cutting edges of a hob, minimizing the organic error of a profile of a generating rack, determining the main parameters for setting up a relieving machine and profile of a grinding circle.

1 Wildhaber-Novikov gears. Parameters of the basic rack

For the first time, helical gears with an initial point tangency of the circular-helical surfaces of the teeth were proposed by the eminent

American inventor E. Wildhaber in 1926 in US Patent No 1,601,750. However, at that time this invention was unnoticed, and such gears received rapid development only after M. L. Novikov had formulated a general principle of their formation and showed that such gears will have the increased load capacity, primarily in a contact endurance [7].

Initially, M. L. Novikov proposed a version of helical overcentre gears, in which tooth profiles, convex on a pinion and concave on a wheel, were delineated with circle arcs in the face section of gears. Later, V. N. Kudryavtsev showed that the same effect could be achieved in the gears synthesized based on two incongruent basic racks with the circle arc profiles and cut by two worm hobs: one for the pinion with convex teeth, the other for the wheel with concave ones [8].

However, at present, basic racks are standardized and widely used in production with a full tooth profile, which provide in gears two lines of action and allow for cutting the pinion and the wheel by one worm hob [9]. In particular, according to the Russian Standard GOST 15023-76, the basic rack consists of a convex addendum, a concave dedendum and a short straight section between them. Geometry of Novikov gears with two lines of action is calculated acc. Russian Standard GOST 17744-72.

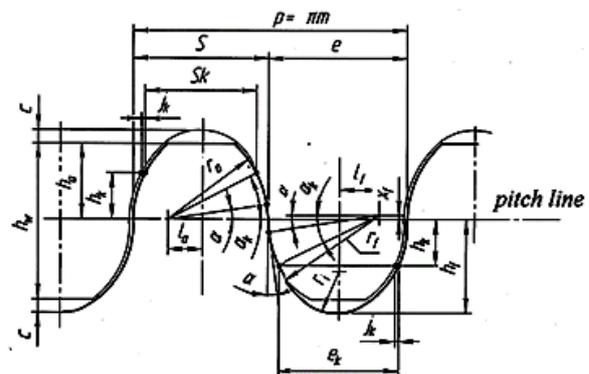


Fig. 1. Basic rack for Novikov gears acc. GOST 15023-76.

Fig.1 shows the main parameters of the basic rack, the values of which depend on the range of modules. The pressure angle α_k at the predetermined contact points on the tooth addendum and dedendum is equal 27° for any case. These points are also characterized by parameters: distance h_k from the pitch line, hob tooth width e_k at its addendum and space width S_k at its dedendum, the difference $j_k = e_k - S_k$ provides a backlash between the teeth of the wheels to be cut. The pressure angle α in the straight section of the tooth depends on the module and is equal to $\approx 8^\circ$.

The hob tooth in the normal section is formed according to the dimensions of the space of the basic rack. Similarly, the space between the hob teeth forms the tooth of the wheel to be cut.

The convex profile of hob tooth is outlined by a radius r_f , the center of curvature of which is located at a distance l_f from the axis of symmetry of the head and is shifted relative to the pitch line to the hob axis by x_f . The center of the concave arc radius r_a of the hob

tooth space is located on the pitch line, at a distance l_a from the axis of symmetry of the space. Dimensions along the pitch line are: the thickness e of the hob tooth and the width S of the hob space. The height h_f of the hob tooth head is equal to the dedendum of the gear to be cut. The depth of the space is equal to the sum of the addendum h_a of the gear and the radial clearance c between the gear and the hob when cutting. Also in Fig.1 the height h_w of the tooth active profile in the gear and the radii r_i of the arc transition curves on the head and in the space of the hob tooth are indicated.

2 Worm hob parameters

The main parameters of any worm hob are: axial module m , radius r_F of the pitch cylinder, number of threads z_0 , screw parameter $p = 0,5m z_0$ of the generating surface, number of teeth z_f in the face section. From this data the lead angle γ_1 of the helical surface of the cutting edges on the hob pitch cylinder is determined from the expression:

$$\tan \gamma_1 = p / r_F \quad (1)$$

The worm hob design profile (a generating rack) is considered in the normal section of the generating worm, which is tangent to the screw front surface. For single-thread hobs this section and front surface practically coincides in the profiling zone.

When teeth are cut on the gear hobbing machine, the plane of the generating rack is installed perpendicular to the direction of the teeth of the cut wheel, while the hob axis is set taking into account the lead angle of the hob front surface.

When the teeth of the worm hob are relieved, its axis is installed in the centers of the grinding-relieving machine, that is, in the horizontal plane. And for a reliable reproduction of the profile of the generating rack in the normal section of the hob, with the adopted profiling method it is necessary to recalculate the parameters of the profile of the generating rack into the axial section of the tooth surface to be relieved.

First of all, it is necessary to determine the axial profile of the helical surface, on which the cutting edges of the hob teeth are located. To do this the prescribed angle α of the normal profile of the straight section should be replaced by an angle α_1 of the axial profile according to the formula:

$$\tan \alpha_1 = \tan \alpha / \cos \gamma_1 \quad (2)$$

The curvature radii ρ_a and ρ_f of the two parts of active profile in the normal section are replaced by the corresponding radii r_{a0} and r_{f0} in the axial section. For single-thread hobs, these radii with a sufficient approximation are determined by the Meunier theorem from the expressions:

$$r_{a0, f0} = \rho_{a, f} / \cos \gamma_1 \quad (3)$$

The arc radius ρ_i on the head of the hob tooth, which is processed fillet of the wheel tooth, in the normal section is replaced with the corresponding radius r_0 in axial section of the hob. According to Euler's formula, these radii are related by the expression:

$$r_0 = \rho_i / \cos^2 \gamma_1 \quad (4)$$

The thread thickness b in the axial section should be determined on the minimum ground radius r_{\min} of the hob, proceeding from the thickness b_n of the normal section at the end point of machining:

$$b = b_n / \cos \gamma_{(r \min)} \quad (5)$$

where $\gamma_{(r \min)} = \text{atan}(p/r_{\min})$ is the lead angle on the hob dedendum cylinder.

The calculated coordinates of the axial profile of the helical surface of the cutting edges are related to the coordinates of the generating rack profile by the dependencies:

- for point A_1 on the tooth dedendum: $x_{01} = x_{n1}$;
 $z_{01} = z_{n1} / \cos \gamma_{x01}$; $\tan \alpha_{01} = \tan \alpha_{n1} / \cos \gamma_{x01}$,
 where $z_{n1} = 0,5\pi m_n + l_a - (r_F - x_{n1}) \cot \alpha_{n1}$; $\gamma_{x01} = \text{atan}(p/x_{01})$,
 - for point A_2 on the tooth addendum: $x_{02} = x_{n2}$; $z_{02} = z_{n2} / \cos \gamma_{x02}$;
 $\tan \alpha_{02} = \tan \alpha_{n2} / \cos \gamma_{x02}$,
 where: $z_{n2} = (x_{n2} - r_F + x_f) \cot \alpha_{n2} - l_f$; $\gamma_{x02} = \text{atan}(p/x_{02})$.

The found parameters of the axial section of the helical surface of the cutting edges of the hob teeth are also parameters of the axial section of the relieved surfaces of the teeth.

For clarity, let us consider Figure 2, which shows an example of the basic rack for gears with the module $m_n = 12$ mm.

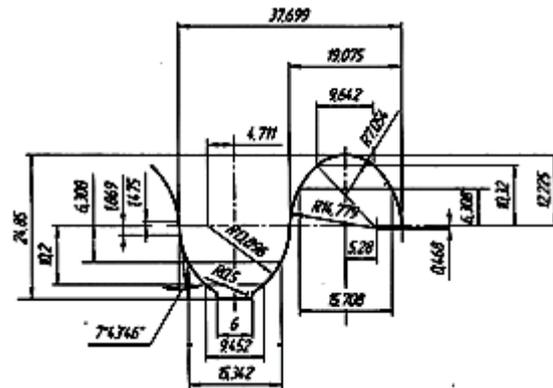


Fig. 2. An example of the basic rack of the hob for gears with the module $m_n = 12$ mm.

For the full-profile Novikov gears, the pitch line of basic rack divides the tooth height by half. The active parts of the hob tooth profile are limited by the dimensions 10.2 and 10.32 mm from the pitch line. At the same points, there is a conjunction of the radius sections of the profile. The tooth thickness in the normal section at the minimum machining diameter is $b_n = 31.7$ mm.

The predesigned parameters of the worm cutter are: the outer diameter of 180 mm, the number of hob threads $z_0 = 1$, the number of teeth in the face section $z_f = 10$, the pitch diameter of 155.55 or its radius $r_F = 77.775$ mm, the fall of the relieving cam on the outer cylinder $K = 10$ mm.

The calculated parameters are: the axial module $m = 12.038$; the screw parameter of the generating worm $p = 6.019$; the lead angle on the pitch cylinder $\gamma_F = 4.425^\circ$; the parameter of relieving $k = Kz_f/2\pi = 15.915$; the minimum radius of grinding on the cylinder of hob spaces $r_{\min} = 66.215$; the lead angle on this cylinder 5.194° ; the maximum tooth thickness $b = 31.83$.

The parameters of the axial profile of the hob generating surface are: the minimum pressure angle on the straight section $\alpha_{1\min} = 7.7523^\circ$; the concave arc radius on the tooth head $r_{of} = 14.823$; the convex arc radius in the space $r_{oa} = 13.938$; the radii of transitive curves on tooth head $r_{if} = 7.096$ and in the space $r_{ia} = 7.002$. The pressure angles at special points of the work area are:

- at a point of conjugation of the radii r_{of} and r_{if} on the head of tooth $\alpha_{0f} = 46.95^\circ$;
 - at the contact point on the head of tooth $\alpha_{01} = 27.35^\circ$;
 - at a point of conjugation of the radii r_{oa} and r_{ia} in the space $\alpha_{0a} = 47.34^\circ$;
 - at the contact point in the space $\alpha_{02} = 27.08^\circ$.

3 Parameters of radial-axial relieving

The hobs for cutting involute gears have an almost straight tooth profile with the pressure angle $\alpha_0 \approx 20^\circ$. The relieving of such hobs is usually carried out by the radial method.

The tooth of hobs for cutting Novikov gears has a substantially curved profile with a large difference in pressure angles. The pressure angle in the straight section of the tooth profile near the

line is $\alpha_0 \approx 8^\circ$, and therefore the rear angles in this section are minimal, which during cutting significantly reduces the wear resistance of the hobs, since it is precisely in this section that they are intensively formed wear sites [10]. In addition to arc sections with large pressure angles, a large shift of the relief surface profile relative to the pitch line will occur, which will appear at re-sharpening of the hob. So such hobs cannot be relieved with a purely radial method and radial-axial relieving must be used.

In general case of radial-axial relieving of the teeth of the worm hob [1, 2] the direction of relieving motion makes up the angle φ_c with the perpendicular to the hob axis, which ensures the obtaining of a necessary rear angle λ_r near the cutting edges of the hob teeth.

The grinding wheel axis O_w-O_w is turned (in the projection to the horizontal plane) at an angle φ_0 to the hob axis O_1-O_1 (see below Fig.5) and is simultaneously inclined to this plane by the angle β_w . Such a method of setting the axis of the grinding wheel eliminates large differences in curvature of the grinding surface of the wheel, improves the grinding conditions and increases the life of the grinding wheel.

During the relieving, the hob rotates around its axis O_1-O_1 with the angular velocity ω_1 , the grinding wheel moves along the hob axis at a speed $p\omega_1$ and performs reciprocating motion with a speed $k\omega_1$, where $k = Kz_f/2\pi$ is the relieving parameter; K is the recession of the Archimedean spiral of the cam of the relieving mechanism on the angular pitch of the hob teeth. The relieving carriage slides are turned relative to the perpendicular to the hob axis by an angle φ_c which allows increasing the rear angle λ_r on the lateral surface of the tooth.

The current radius r_w of the grinding wheel is determined at the point of its contact with the tooth of the hob on its current cylinder. For the initial position of the wheel, it is advisable to take the tangency of its maximum radius $r_{w\max}$ with the minimum radius of the work piece surface $r_{i\min}$.

With radial-axial relieving, the lead angle γ_0 of the relieved surface at each of two selected points ($i_{1,2}$) is determined from the expression [1, 2]

$$\tan\gamma_{0i} = [p \pm k \sin(\alpha_i + \varphi_c) / \cos \alpha_i] / x_{0i} \quad (6)$$

where the radius x_{0i} of the location of the selected point on the ground surface is determined from the drawing of the product.

The sign "+" in square brackets refers to the teeth side where the lead angle of the relieved surface is greater than the lead angle of the generating surface of the hob, sign "minus", respectively, to the opposite side of the teeth.

From formula (6) it follows that the values of the angles γ_{0i} depend on the angle φ_c of the installation of the relieving support, which is determined by the required rear angle near the cutting edge of the tooth. For hobs with variable profile curvature, this angle is determined at the location of smallest value of angle α_{0i} and equal to $\alpha_{0\min}=7.7523^\circ$ in the considered example for a straight line segment near the pitch line.

4 Calculation of the angle φ_c installation of the relieving support of the machine

For worm hobs intended for finish cutting of involute gears with module 12 mm of the thermally hardened steels, the Russian State Standard 9324-80 recommends radial relieving parameters providing the normal relief angle on a pitch cylinder $\approx 4^\circ$. Based on this recommendation, for the considered type of hobs, we establish the following dependence, which ensures the determination of φ_c with the sufficient accuracy for practical calculations:

$$(\tan \gamma_{0F} - \tan \gamma_{xF}) \cos \alpha_{0\min} = \tan 4^\circ \quad (7)$$

Expanding the meanings of $\tan \gamma_{0F}$ from (6) and $\tan \gamma_{xF} = p/r_F$, we obtain the following expression for determining the value of φ_c

$$\sin(\alpha_{0\min} + \varphi_{cR,L}) = 0,44 r_F / (Kz_f) \quad (8)$$

Indexes R, L relate to the right and left sides of the hob tooth. For the example considered above with $\alpha_{0\min}=7.7523^\circ$ we obtain $\varphi_{cR,L}=12.229^\circ$. Taking into account the price of rotation angle scale we set according to the rounding rules $\varphi_{cR,L}=12^\circ$.

Table 1 shows the calculated parameters of the profile of the hob tooth and the lead angles of the relieved surface of the teeth at seven key points of the profile $i=1...7$:

- 1 - the boundary of the active section of the profile on the tooth leg,
- 2 - the contact point on the dedendum of the hob tooth,
- 3 - the conjugation of the arc concave section with a rectilinear section,
- 4 - the point on the hob pitch cylinder,
- 5 - the conjugation of the rectilinear and arc sections on the tooth head,
- 6 - the contact point on the addendum of the hob tooth,
- 7 - the boundary of the active section of the profile on the tooth head.

Table 1. Parameters of hob tooth profile in key points (for the given example).

№ p/p	Radius of point, mm $x_i=r_i$	Pressure angle in axial section, α_{0i}°	Lead angle of screw surface of cutting edges, γ_i°	Lead angles of relieved surface on the tooth sides:	
				right, γ_{0iR}°	left, γ_{0iL}°
1	67.575	47.338	5.09	21.207	-11.853
2	71.467	27.079	4.814	13.598	-4.200
3	75.906	7.752	4.587	8.576	0.446
4	77.775	7.752	4.425	8.373	0.435
5	79.25	7.752	4.343	8.219	0.427
6	84.083	27.35	4.094	11.679	-3.635
7	88.095	46.951	3.909	16.439	-9.001

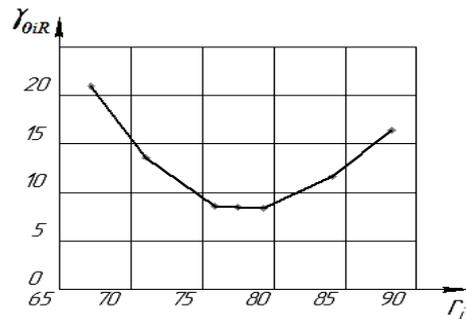


Fig. 3. Diagram of the function $\gamma_{0iR} = f(r_i)$ - right flank.

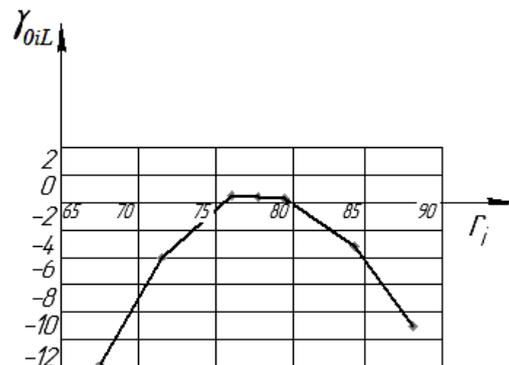


Fig. 4. Diagram of the function $\gamma_{0iL} = f(r_i)$ - left flank.

plane (downwards when processing the right side of the tooth). Its value reaches maximum at the extreme point of intersection of the face sections of the outer wheel cylinder (radius r_{wm}) and the cylinder of the hob radius (r_F+h_k) at the contact point on the tooth head. The distance from this point to the horizontal plane for simple geometric reasons is determined by the formula:

$$l_{max} = r_{wm} \sin \psi, \tag{14}$$

where
$$\psi = \arccos \frac{r_{wm}^2 + (r_{wm} + r_{min})^2 - (r_F + h_k)^2}{2r_{wm}(r_{wm} + r_{min})} \tag{15}$$

The linear displacement Δ of the back surface of the grinding wheel to the middle of the space at a length l_{max} in a screw projection onto the axial plane of the cutter to both tooth sides will be:

$$\Delta_{R,L} \approx \pm l_{max} [\tan \beta_{wR,L} \cos \varphi_0 - p / (r_F + h_k)] \tag{16}$$

where the sign “+” relates to right side of the right-hand hob, the sign “-“ to its left side.

In the angular dimension, this displacement is determined from the expression:

$$\tan \varphi_\beta = \Delta / (r_F + h_k) \tag{17}$$

The pruning of the cutting edges of the opposite side of the thread is guaranteed to be excluded if condition $\varphi_0 + \varphi_\beta \leq \alpha_{0i}$ is met, where the value α_{0i} is accepted for the key point 6 from Table 1. For preliminary calculation of the relieving parameters, the angle φ_0 should be taken equal to $\varphi_0 = 18^\circ$. Then, having determined the angle φ_β by formula (19), it is possible to correct the angle φ_0 by increasing it to the maximum permissible value

$$\varphi_{0max} = \alpha_{0i} - \varphi_\beta \tag{18}$$

Given that increasing φ_0 reduces the needed value of the angle β_w , such an adjustment is advisable.

As an example, we will calculate the relieving parameters β_w and φ_0 as applied to the hob considered above, and study the features of the resulting side surfaces.

As the initial points for constructing the designed normals, we take the points: on the leg A_1 , at the contact point with pressure angle $\alpha_{01} \approx 27^\circ$ (key point 2 from table1), on head A_2 at the conjugation between the active profile and the transition curve with the angle $\alpha_{02} \approx 47^\circ$ (key point 7). The coordinates of these points and the exact values of the pressure angles are in table 1.

The maximum radius of the grinding wheel is assumed to be equal to $r_{wm} = 60$ mm, the minimum radius of the relieved surface on the space $r_{min} = 66.215$ mm, the height of the grinding profile of the hob tooth is $H_1 = 23.785$ mm for both sides of the teeth of the manufacturing surface. The value of the turning angle of the relieving support to provide a rear angle in the middle section of the profile $\varphi_c = 12^\circ$ for both sides of the teeth.

The lead angles γ_{0i} of the relieved surface at the points A_1 and A_2 were shown in table 1 for each side of a tooth of the right-hand hob. On the right side of the tooth, at which the lead angle of the relieved surface is greater than the lead angle of the generating worm they are equal $\gamma_{01} = 13.598^\circ$, $\gamma_{02} = 6.439^\circ$. On the opposite, for the left tooth side we have $\gamma_{01} = -4.200^\circ$, $\gamma_{02} = -9.001^\circ$.

Negative values of lead angles γ_{0i} of the relieved surface at the points of arc sections of the profile mean its transformation in these sections into an analogue of the left helical surface, which is characteristic for single-thread hobs with a standard lateral rear angle of 4° or more, with the number of modules in the pitch diameter of 12 or more.

Table 2 summarizes the main stages of the calculations by means of the corresponding formulas.

Table 2. Calculation of the parameters β_w and φ_0 of the hob teeth.

Data	Formula number	Estimated Values		
		preliminary		final
		Right	Left tooth side	
φ_0°		18.0	18.0	19.0
a ,	(9)	134.47	134.47	135.15
x_1	(12)	107.76	107.76	107.21
z_1	(11)	82.21	82.21	81.14
y_1	(12)	17.17	-5.17	-5.13
x_2	(12)	122.47	122.47	122.44
z_2	(11)	36.94	36.94	36.91
y_2	(12)	9.47	-5.09	-5.08
β_w°	(13)	9.19	-0.095	-0.064
ψ°	(15)	34.64	34.64	34.64
l_{max}	(14)	34.11	34.11	34.11
Δ	(16)	2.81	2.49	2.47
φ_β°	(17)	8.93	7.95	7.89
φ_{0max}°	(18)	18.42	19.40	19.46

For the right side, the difference between the values of the initial φ_0 and the adjusted φ_{0max} angles in the preliminary calculation is less than 1° , therefore, a change in φ_0 is not required. For the left side, the final calculation is carried out by increasing the angle φ_0 to 19° , and recalculation of β_w , which however has changed very slightly and which in practice in both cases is rounded to the value -0.1° .

In [1, 2] it was shown that the discrepancy between the profiles of the grinding wheel surface and the hob tooth flank to be ground will be minimal if in the vicinity of the calculated contact point, the line of their contact will not be crossing the axial section of the hob, but touching it. This condition is satisfied in the case when the axis of the grinding wheel is inclined to the axial plane at an angle β_w , which is determined depending on the pressure angle α_0 , the lead angle γ_{0i} and the radius r_i of the relieved surface, taking into account the installation angle φ_0 of the wheel axis in the projection onto the horizontal plane, by the expression:

$$\tan \beta_w = \tan \gamma_{0i} \cos \alpha_{0i} / \cos(\alpha_0 + \varphi_0) \tag{19}$$

Table 3 shows the values of the angle β_w calculated according to this dependence for seven key points of the axial section of the right and left sides of the hob teeth.

Table 3. Values of the angle β_w calculated for the different sides of the hob tooth.

Point numbers	1	2	3	4
x_{0i} , mm	67.575	71.467	75.906	77.775
α_{0i}°	47.34	27.08	7.75	7.75
γ_{0i}° (right side)	21.207	13.598	8.576	8.373
β_w° (right side)	32.22	16.96	9.42	9.198
γ_{0i}° (left side)	-11.853	-4.20	0.446	0.435
β_w° (left side)	-18.882	-5.29	0.491	0.479
Point numbers	5	6	7	
x_{0i} , mm	79.25	84.083	88.095	
α_{0i}°	7.75	27.35	46.95	
γ_{0i}° (right side)	8.219	11.679	16.439	
β_w° (right side)	9.029	16.641	25.441	
γ_{0i}° (left side)	0.427	-3.625	-9.001	
β_w° (left side)	0.470	-4.590	-14.325	

In Fig. 6 (upper part) a graphical interpretation of the dependence (19) of the angle β_w on the hob radius is given for the right side of the teeth. Let us draw two boundary straight lines: one through the starting points A_1 and A_2 of the designed normals, and

the second horizontal line at minimum value $\beta_w = 9.19^\circ$ (from Table 3) until they mutually intersect in some point C. The sections of the profile that fell into the sector between the boundary lines have practically no organic error, since any straight line drawn through the intersection point C inside the sector also pass through two points of the axial profile of the relieved surface. Outside the obtained sector, the relieved profile has a small organic deviation from the given profile of the grinding wheel.

At the lower part of Fig. 6 a similar dependence of the angle β_w on the hob radius is shown for the left side of the teeth. One boundary straight line passes through the points of the line corresponding to the values of the radius at points A_1 and A_2 . The second line runs horizontally, touching the line at its upper point with a value of $\beta_w = -0.1^\circ$. The intersection of these lines forms a sector in which the organic deviation of relieved profile is practically absent.

8 Profiling of grinding wheels

Significant difficulties in the manufacture of worms and worm hobs with a profile of substantial and variable curvature are due to the fact that the circle dressing copiers included in the delivery of grinding machines are not suitable for reproducing such a profile [1, 2]. At present, with the development of CNC, ruling devices with diamond rollers and programmed control of their movement relative to the working surface of the grinding wheel have gained a certain distribution.

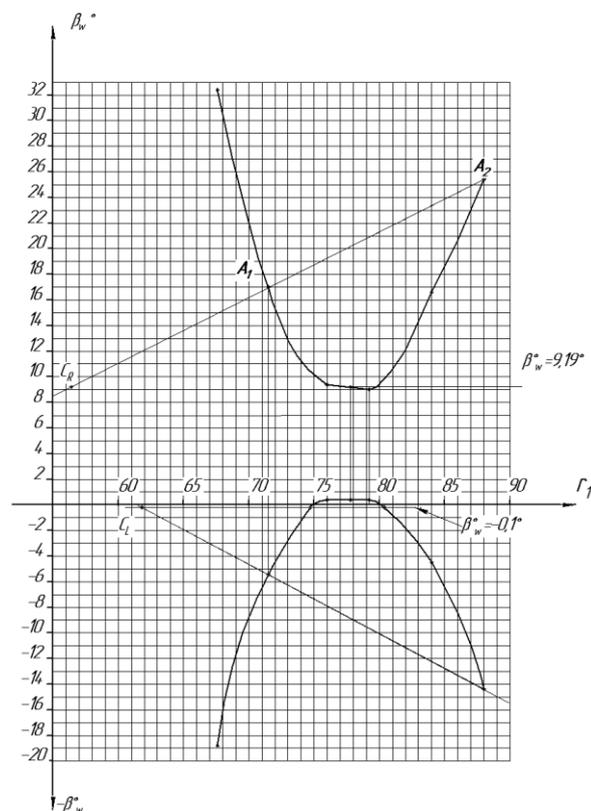


Fig. 6. Angles β_w vs. the current radius of the hob.

The characteristic of the surface of the grinding wheel, i.e., the line of its contact with the surface to be ground, is oriented along the axial section of the latter. Therefore, profiling of the wheel in its axial section with a sufficient degree of approximation reproduces the section of the surface being ground that is normal to a helical line with the lead angle equal to β_w . That is, the axial profile of the grinding wheel for single-thread hobs practically repeats the profile of the basic rack. In this case, the value of the angle α_w of the wheel profile in a rectilinear section is determined from the expression:

$$\tan \alpha_w = \tan(\alpha_{0\min} + \varphi_0) \cos \beta_w \quad (20)$$

In general, the coordinates of the axial profile of the grinding wheel, based on the coordinates of the axial section of the relieved surface of the hob teeth, the lead angles of this surface and the found angle of inclination of the wheel axis, are determined by the following expressions:

$$\begin{aligned} z_w &= z_{0i} / (\cos \beta_w + \tan \gamma_{0i} \sin \beta_w); \\ x_w &= x_{0i} + z_n^2 \sin 2\beta_w \tan \gamma_{0i} / (4x_{0i}). \end{aligned} \quad (21)$$

9 Sensitivity to the hob regrinding

If the relieving of surfaces with a variable curvature profile is performed by the radial-axial method, then the axial component $k_x = k \sin(\alpha_{0i} + \varphi_c) / \cos \alpha_{0i}$ of the relieving parameter included in formula (6) is variable along the profile. In this case, strictly speaking, the profile distortion during regrinding of the hob teeth on the front surface is inevitable. However, the considered profile has the points with identical pressure angles α_{0i} (for example, at the conjugate points of large and small radii on the tooth head and leg) and the lead angles γ_{0i} of the relieved surface, and therefore, at these points and in the areas between them, the profile deviations as regrind are minimal.

Conclusion

The relieving process for tooth flanks of worm hobs for cutting Novikov gears with two lines of action has been studied. The results of this research are shown below.

1. Change of the relieved surface lead angle of hob teeth has a parabolic dependence on the radius and pressure angle of the tooth profile. The relieved tooth surfaces of such hobs are organically characterized by the presence of paired profile points with the equal lead angles.

2. The minimum rear angle of the hob teeth takes place near the hob pitch cylinder, and the installation angle φ_c of the relieving support of the grinding-relieving machine is necessary to be calculated based on the minimum value of the rear angle 4° .

3. For both right and left sides of the teeth it is preferable to assign the installation angle φ_0 for the grinding wheel axis at 18° . Also, pruning on the opposite side of the generating surface of the cutting edges has to be prevented.

4. At the relieving of the left side of the right-hand hob teeth the directions of the lead angles of the relieving surface and the helical surface of the cutting edges have different signs. Accordingly, the angle β_w of inclination of the grinding wheel axis to the horizon can also have a sign opposite to the lead angle γ_1 of the hob generating surface.

The technique has been developed for calculating the parameters of installation, movement and profile of the disk grinding wheel for the relieving process of the tooth flanks. In the axial section of the hob it allows to obtain at least 4 points of contact between the wheel and the surface to be ground. Thus, the organic grinding error is minimized during the profiling of the grinding wheel, and generated profile is as close as possible to the profile of the hob basic rack.

The above technique is also proposed to be used in the development of control programs to set up the grinding-relieving machine and the dressing mechanism of the grinding wheel for worm hobs manufacturing on relieving machines with the numerical program control.

References

1. S.A. Lagutin and A.I. Sandler, Grinding of Helical and Relieved Surfaces, Publishing House "Mashinostroyeniye". (1991)

2. A.I. Sandler, S.A. Lagutin and A. V. Verhovski, Manufacturing of Worm Gears, Publishing House "Mashinostroyeniye" 272 p. (2008)
3. A.I. Sandler, S.A. Lagutin and E.A. Gudov, Theory and Practice of Manufacturing of General Type Worm Gears, Publishing House "Infra-Engineering" Moscow-Vologda (2016).
4. F.L. Litvin and A. Fuentes, Gear Geometry and Applied Theory, Cambridge University Press (2004)
5. A.I. Sandler and S.A. Lagutin, Features of Forming Screw and Relief Surfaces for Fluid Friction Worm Gears, *International Symposium on Theory and Practice of Gearing*, Izhevsk, pp. 375-380 (2014)
6. A.I. Sandler and S.A. Lagutin, Relieving the teeth of hobs for cutting the Wildhaber-Novikov gears. *The 10th International Conference KOD 2018 "Machine and Industrial Design in Mechanical Engineering"*, Novi Sad, Serbia / IOP Conference Series: Materials Science and Engineering, Volume 393, (2018)
7. M.L. Novikov, Gears with New Engagement, Publ. VVIA n.a. Zhukovsky (1958)
8. V. N. Kudryavtsev, On the issue of Novikov Gearing. In: *Research and mastering of gears with Novikov gearing*. Publ. House of the USSR Academy of Sciences. pp 33-44. (1960)
9. V.I. Korotkin, N.P. Onishkov and Yu. D. Kharitonov Novikov Gearing: Achievements and Development, Nova Science Publishers (2011)
10. Yu. N. Stebletsov. A.S. Tarapanov, Wear resistance of the cutting tool when processing Novikov gears. In: *Fundamental and applied problems of engineering and technology* - Orel: State University - UNPK, - №4 / 3. Pp. 83-86 (2011)